

## ORIGINAL RESEARCH ARTICLE

## DFT Investigation of Magnesium-Doped Zirconolite for High-Level Nuclear Waste Immobilization

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## ABSTRACT

The black mineral zirconolite ( $\text{CaZrTi}_2\text{O}_7$ ), which is made up of calcium zirconium titanate, has been considered an appropriate waste form for immobilizing radioactive waste. Using Density Functional Theory (DFT), this study examined the impact of magnesium substitution on ceramic nuclear waste from Zirconolite. To explore the material's structural stability and electronic characteristics, a computational simulation was conducted using Quantum ESPRESSO within the Perdew-Burke-Ernzerhof generalized gradient approximation (PBE-GGA) and Broyden-Fletcher-Goldfarb-Shannon (BFGS) relaxation calculations. From the energy range of -2.0 eV to 2.0 eV, the computed electronic band structure was displayed along the symmetry routes. An indirect band gap material with 0.06 eV was revealed by the energy gap between the valence band maximum (V<sub>BM</sub>) and the conduction band minimum (CB<sub>m</sub>) at the R<sub>2</sub> and  $\Gamma$  sites. The behavior of semiconductors is consistent with this energy gap value. The dopant substitution energy effect was determined to be 1.424 eV, indicating that the Mg-doped Zirconolite's molecular structure remained stable. To sum up, doping  $\text{CaZrTi}_2\text{O}_7$  ceramic may promote the production of oxygen, which enhances Magnesium's mobility to the subterranean water molecules inside the geological disposal facility.

## INTRODUCTION

The world is currently facing serious issues relating to greenhouse gas emissions (GHGs) caused by global warming due to energy production (Musa et al., 2022) (Aliyu et al., 2024). The production of clean energy is crucial to support the everyday life of human beings and to drive economic growth and development. Recently, to meet the requirements of clean energy generation, nuclear energy has become a preferable option and has been broadly investigated due to its high energy density, low-cost, and absence of air pollution (Hurley et al., 2022; Mathew, 2022). While we cannot completely rely on renewable energy sources, the applications of nuclear reactors as a major energy source can secure the disposition of spent nuclear fuel, and this can ultimately represent the future of clean energy (Pastina and Laverne, 2021). Radionuclides are finding increasing applications in the fields of medicine, chemical industry, and agriculture but produce radioactive waste materials in the process. In terms of the production and operation of the nuclear fuel

cycle, radioactive waste by-products generated are potentially harmful (Subba Rao et al., 2022).

High-level radioactive waste (HLW) as a nuclear power plant's by-product has threatened the public and the environment (Ma et al., 2018). The current solutions include reprocessing through *mixed oxide* (MOX), fuel conversion, and immobilization by direct disposal in the Geological Disposal Facility (GDF) (Schreinemachers et al., 2022; Tanti and Kaltsoyannis, 2021). Among the different solutions, immobilization is crucial to mitigate this issue. Immobilization refers to waste transformation by atomistic replacement of radioisotopes inside a waste form. Nuclear waste substances provide different conditions comprising long-term stability, leaching endurance, and high waste stacking. Based on the category of the waste to be incorporated, a waste form must provide chemical flexibility to incorporate many radionuclides and impurities as well as a high tolerance

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against radiation damage (Neumeier *et al.*, 2017). For instance, borosilicate glasses have been used as an HLW immobilization matrix globally, and exciting results have been achieved (Jafar *et al.*, 2021). However, minor actinides, less solubility, lower activity loading, and devitrification are the limitations of glass matrices. Synroc is proposed as an analogue titanate mineral that can replace borosilicate glasses for HLW immobilization. Synroc entails zirconolites, perovskites, hollandites, pyrochlore and rutile type phases. Zirconolite is a naturally occurring titanate ceramic and the main holding phase for actinides among synroc ceramic waste forms (Blackburn *et al.*, 2020; Blackburn *et al.*, 2021).

Zirconolites have been preferred among ceramic waste forms due to their efficiency in aqueous stability, chemical malleability, waste packing, and radiation hardness (Ma *et al.*, 2018; Shuaibu *et al.*, 2020). It has a stoichiometry of  $\text{CaZr}_x\text{Ti}_{3-x}\text{O}_7$  for  $0.85 \leq x \leq 1.30$  in a monoclinic crystal structure (zirconolite-2M) with a  $C2/c$  space group (Blackburn *et al.*, 2020). In addition, Zirconolite revealed various polytypes properties related to stacking order among  $\text{CaO}_8/\text{ZrO}_7$  polyhedra and  $\text{TiO}_6$  due to lanthanide/actinide integration and fractional oxygen pressure as reported (Wen *et al.*, 2021). Experimentally, various oxidation states and ionic radii of actinides and lanthanides have been potentially doped within zirconolite-2M through substitution schemes consisting of direct and charge-compensated substitutions (Jafar *et al.*, 2014). The lanthanide/actinide ions with a valency of 3+ or 4+ might directly replace Ca, Zr, and/or Ti sites in direct substitution. For charge-compensated substitution, Ca and/or Zr sites may be replaced by the lanthanides or actinides after substituting Ti sites with a charge-compensated ion to neutralize the charges (Loiseau *et al.*, 2003; Whittle *et al.*, 2012). Many literatures have presented studies on the charge-compensated substitution mechanism in the zirconolite-2M phase. The charge-compensated ions comprise Cs,  $\text{Mg}^{2+}$ ,  $\text{Al}^{3+}$ ,  $\text{Fe}^{3+}$ , and  $\text{Nb}^{5+}$  (Lago *et al.*, 2022; Ma *et al.*, 2018; Zhou *et al.*, 2022).

Interestingly, the properties of a material can be improved by doping, that is, the introduction of impurities within a chemical structure to tune the properties of the material. The doping strategy has been widely reported to potentially alter materials' physical and chemical properties (Haruna *et al.*, 2020; Ilie *et al.*, 2018). Tanti and Kaltsoyannis (2021) investigated the effects of doping actinides and Ce into Zirconolite employing periodic DFT and molecular dynamics simulation (MD). The results indicated a redox behaviour and solid correlations between the ions' substitutional energies, a ratio of substituents ionic radius, and substituted ions.

The incorporation of trivalent at the Ti site has been investigated widely, indicating phase evolution and solubility of lanthanide/actinides in zirconolites (Zhou *et al.*, 2022).

However, no effect of divalent such as  $\text{Mg}^{2+}$  incorporation at the Ti site regarding phase evolution and lanthanide/actinides solubility was investigated. Magnesium (Mg) has been widely known as the natural constituent of zirconolite mineral and spent nuclear fuel (Barlow *et al.*, 2021; Zhou *et al.*, 2022). The Mg incorporation into Zirconolite would affect radionuclides' solubility limits and substitution mechanism. To the best of our knowledge, this is the first first-principle investigation to highlight Mg incorporation into Zirconolite.

## COMPUTATIONAL DETAILS

The computations are conducted on the  $2 \times 2 \times 2$  supercells comparative to the standard primitive unit cell of Magnesium doped Zirconolite  $\text{CaZrTi}_2\text{O}_7$  within ab-initio calculation using Quantum ESPRESSO simulation package (QE) (Lawal *et al.*, 2018). Electron-electron interactions were treated using Perdew-Burke-Ernzerhof's generalized gradient approximation (PBE-GGA) (Perdew *et al.*, 1996). Integrals were evaluated using Maxfessel-Paxton's smearing method.  $6 \times 6 \times 6$  k-points grids for all the materials and 50 Ry has been chosen for the kinetic energy cut-off based on the Monkhorst-Pack scheme for the Brillouin zone integration. Also, XCrysdn (X-window Crystallin Structure and Densities) a program for visualization for electronic and structural analysis, was applied (Shuaibu *et al.*, 2021). The supercells relative to the primitive unit cell were applied, consisting of forty-four atoms: four Calcium atoms, four Zirconium atoms, eight Titanium atoms, and twenty-eight Oxygen atoms. One Titanium (Ti) atom was substituted by a Magnesium atom, giving 12.5 % possession by the dopant. The supercell dimensions were maintained for the whole calculations, while the atomic positions were relaxed for all calculations using Broyden-Fletcher-Golfarb-Shannon (BFGS) algorithm, till the acting forces on the atoms reduced to  $0.001 \text{ eV}/\text{\AA}$ .

## RESULTS AND DISCUSSION

### 1.1 Convergence Test Results of Magnesium-doped $\text{CaZrTi}_2\text{O}_7$

Principal computations are computed based on convergence tests as a main requirement for DFT calculations (Shuaibu *et al.*, 2020). Figure 1 shows the convergence results of Mg-doped Zirconolite, indicating variation of the total energy ( $E_{\text{tot}}$  (Ry)) with respect to ( $E_{\text{cut}}$  (Ry)). The Figure shows a sharp decrease in total energy as cut-off energy increases. However, the two measure turning points at  $E_{\text{cut}}$  of 30 and 40 Ry respectively. Furthermore, the total energy remains almost constant between  $E_{\text{cut}}$  of 50 and 70 Ry. Therefore, 50 Ry is considered as an optimized kinetic energy cut-off for Mg-doped Zirconolite.

## 1.2 Structural properties of Magnesium-doped $\text{CaZrTi}_2\text{O}_7$

Zirconolite structure with a space group  $PI$  showed triclinic geometry with high symmetry from which eight oxygen atoms are bonded to each Ti atom. It can be observed from Table 1 that eight various symmetrical approaches exist for 12.5 % of substitutional doping cases. In each case, Ti atoms can be substituted by Mg atoms (Figure 3). However, the  $D_8_{0.125}$  configuration was considered for this particular study, and no structural changes were observed. Hence, the crystal parameters stayed stable. To obtain the stability of the structure after doping, the dopant formation energy (substitution energy) of the Mg atom was computed using (1) (Shamsudeen *et al.*, 2019). The substitution energy means the energy required to insert one Mg atom with a chemical potential  $\mu_{Mg}$  into the supercell after removing one of the Ti atoms with chemical potential  $\mu_{Ti}$  from the same position (Hanaor *et al.*, 2012).

$$E_s = E_{doped} - E_{undoped} + \mu_{Ti} - \mu_{Mg} \quad (1)$$

Where,  $E_{doped}$  is the total energy of the Mg-doped zirconolite  $\text{CaZrTi}_2\text{O}_7$  material;  $E_{undoped}$  is the total energy of the total energy of the undoped Zirconolite  $\text{CaZrTi}_2\text{O}_7$  system;  $\mu_{Ti}$  is the chemical potential per atom of Ti bulk crystal;  $\mu_{Mg}$  is the chemical potential per atom of Mg bulk crystal. The chemical potential was numerically computed as the DFT total energy per atom in the bulk systems (Shamsudeen *et al.*, 2019). The dopant substitution energy of the  $\text{CaZrTi}_2\text{O}_7$ -Mg was determined a 1.424 eV (from Table 2) and it evaluates the degree of stability of the doped structure. The lesser the substitution energy, the greater the stability of a structure. Therefore, the Mg-doped  $\text{CaZrTi}_2\text{O}_7$  has demonstrated a stable structure based on the calculated value of the substitution energy.

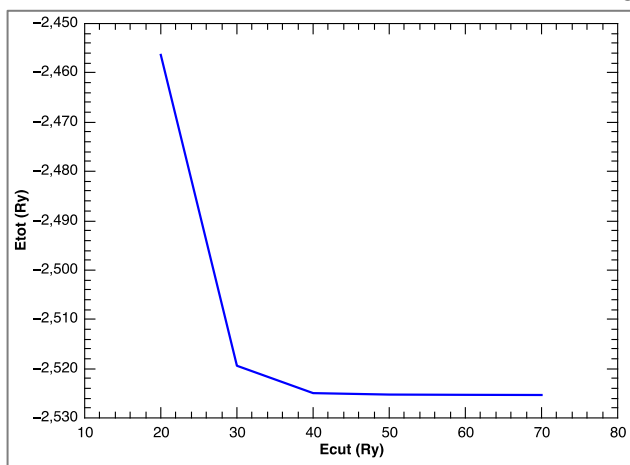


Figure 1. The convergence of total energy with respect to the kinetic energy cut-off.

Figure 2 shows the variation of total energy ( $E_{tot}$  (Ry)) versus the k-points mesh. The  $E_{tot}$  reduces significantly as the k-points mesh increases from  $2 \times 2 \times 2$  to  $6 \times 6 \times 6$ . However, the  $E_{tot}$  was maintained from  $6 \times 6 \times 6$  to  $12 \times 12 \times 12$ . Therefore,  $6 \times 6 \times 6$  is considered an optimized k-point for Mg-doped Zirconolite (Appendix A; Table A1).

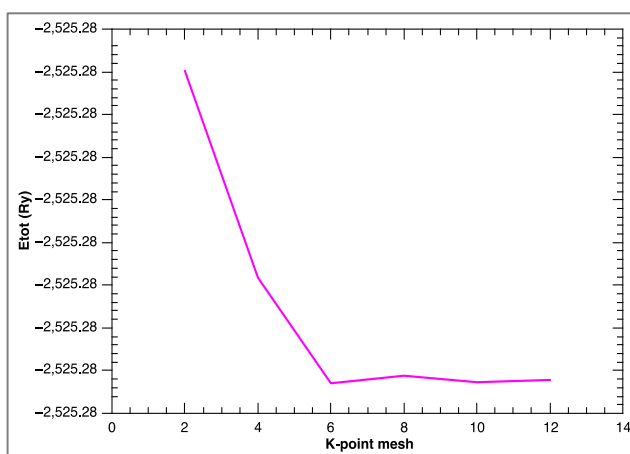


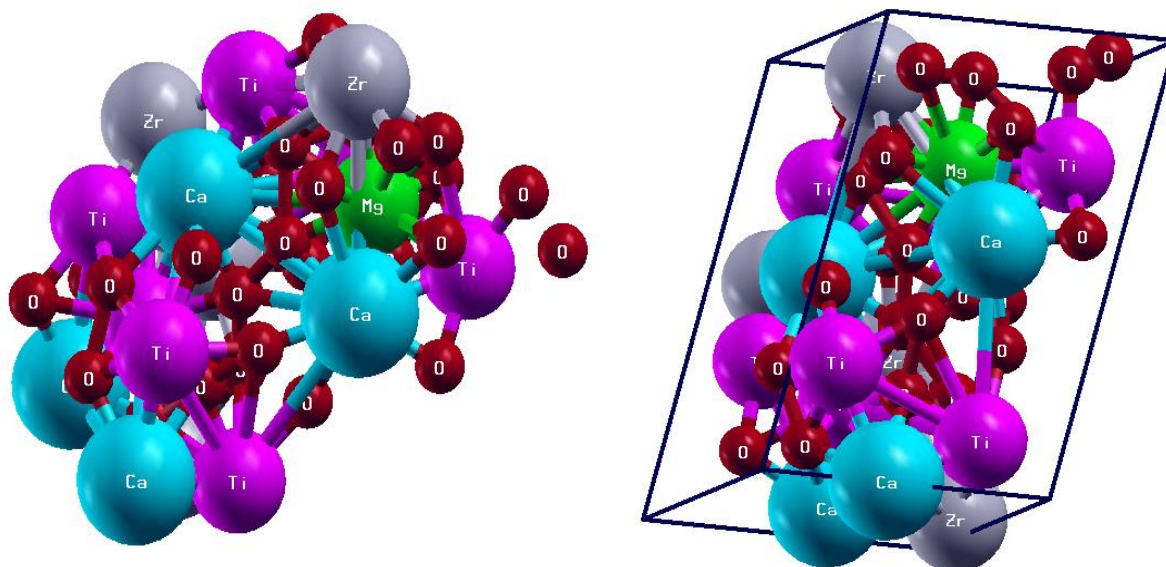
Figure 2. The convergence of the total energy with respect to the k-points grids.

Table 1: Configurations for substitutional doping of Ti by Mg zirconolite  $\text{CaZrTi}_2\text{O}_7$  material.

Undoped	Ti	Ti	Ti	Ti	Ti	Ti	Ti	Ti	Ti
$D_{1_{0.125}}$	Mg	Ti	Ti	Ti	Ti	Ti	Ti	Ti	Ti
$D_{2_{0.125}}$	Ti	Mg	Ti	Ti	Ti	Ti	Ti	Ti	Ti
$D_{3_{0.125}}$	Ti	Ti	Mg	Ti	Ti	Ti	Ti	Ti	Ti
$D_{4_{0.125}}$	Ti	Ti	Ti	Mg	Ti	Ti	Ti	Ti	Ti
$D_{5_{0.125}}$	Ti	Ti	Ti	Ti	Mg	Ti	Ti	Ti	Ti
$D_{6_{0.125}}$	Ti	Ti	Ti	Ti	Ti	Mg	Ti	Ti	Ti
$D_{7_{0.125}}$	Ti	Ti	Ti	Ti	Ti	Ti	Mg	Ti	Ti
$D_{8_{0.125}}$	Ti	Ti	Ti	Ti	Ti	Ti	Ti	Ti	Mg

Table 2: Calculated total and Fermi energy of pure and Mg-doped  $\text{CaZrTi}_2\text{O}_7$

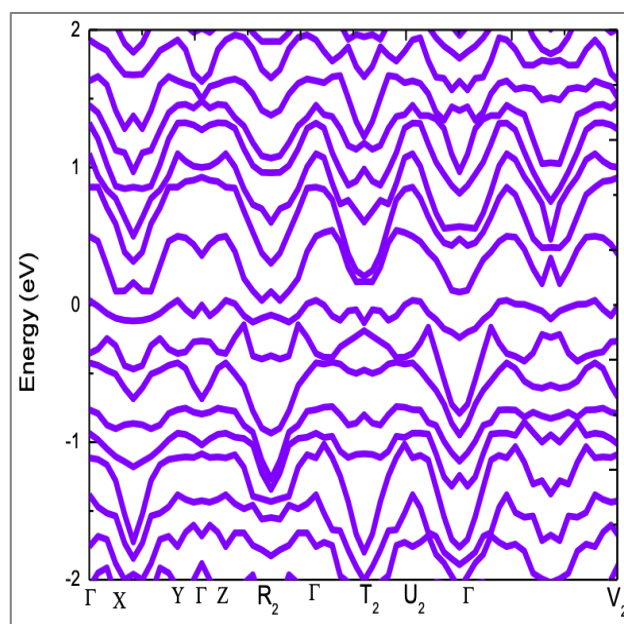
Material	Total energy (Ry)	Fermi energy (eV)
Pure $\text{CaZrTi}_2\text{O}_7$	-2569.44129866 (Shuaibu <i>et al.</i> , 2020)	9.6918 (Shuaibu <i>et al.</i> , 2020)
Mg-doped $\text{CaZrTi}_2\text{O}_7$	-2525.27914843	42.9868 (This work)



**Figure 3.** The bulk structure of simulated Mg-doped Zirconolite: red (small dark) spheres show oxygen ions, grey (large grey) spheres show zirconium ions, cyan (large cyan) spheres show Calcium ions, and purple (large purple) spheres show Ti ions, green (large green) show Magnesium.

### 3.2 Electronic Properties of Magnesium-Doped Zirconolite

The determination of the electronic properties of a material is important to allow the interpretation of the solid's properties (Lawal *et al.*, 2018; Radzwan *et al.*, 2020). The investigation of electronic properties of Mg-doped Zirconolite comprises the electronic band structure, density of state (DOS), partial density of state (PDOS), and charge density distribution. Mg was added to pure  $\text{CaZrTi}_2\text{O}_7$  in the calculations targeting the Ti side to understand the effects of doping. Each Mg atom substitutes one of the Ti atoms on the  $\text{CaZrTi}_2\text{O}_7$  perfect crystal plane, and the Mg atom is joined with the Ti atoms to make Ti-Mg bonds. The calculated electronic band structures of Mg-doped  $\text{CaZrTi}_2\text{O}_7$  are shown along the eleven symmetry ( $\Gamma-X | Y-\Gamma-Z | R_2-\Gamma-T_2 | U_2-\Gamma-V_2$ ) directions, and the energy of band structure separation is plotted from  $-2.0 \text{ eV}$  to  $2.0 \text{ eV}$  (Figure 4). The Fermi level is the zero-energy scale on the band structure. A generalized gradient approximation (PBE-GGA) was preferred over Local Density Approximations (LDA) due to its reliability and accuracy in DFT calculations. The energy partition between the CBm and the VBm occurred at  $R_2$  and  $\Gamma$  points, respectively, indicating an indirect band gap material with a  $0.06 \text{ eV}$  energy gap. The energy band gap revealed its semiconductor behaviour. It is worth noting that the energy band gap reduces considerably with the undoped simulated Zirconolite found at  $2.90 \text{ eV}$  as shown in Figure 4.



**Figure 4.** Calculated band structure of Magnesium (Mg) doped Zirconolite ( $\text{CaZrTi}_2\text{O}_7$ ) compound.

Total DOS and PDOS were studied to understand clearly the nature of the energy gap. DOS describes the number of states per each energy level available for occupation and the nature of the band gap, and PDOS explains the origin of the valence and conduction band (Shuaibu *et al.*, 2021). Figure 5 shows the DOS and PDOS results, respectively. Both figures illustrate the presence of higher and lower peaks at the conduction band and the valence band. The lowest valence states are dominated by  $\text{Ca-}3s$ ,  $\text{Zr-}4s$ ,  $\text{Ti-}3s$ ,  $\text{Mg-}2s-2p$ , and  $\text{O-}2s$  orbitals which occurred approximately within  $(0.0 \text{ eV to } -4.0 \text{ eV})$ . The  $\text{Ca-}3s$ ,  $\text{Zr-}4s$ ,  $\text{Ti-}3s$ ,  $\text{Mg-}2p$ ,

and  $O-2p$  orbitals highly contributed in the conduction band for  $Mg$ -doped  $CaZrTi_2O_7$  (0.0 eV to 4.0 eV). The major contribution of the valence band close to the Fermi level is from  $Ca-3p$ ,  $Zr-4p$ ,  $Ti-3p$ , and  $O-2p$  orbitals. The

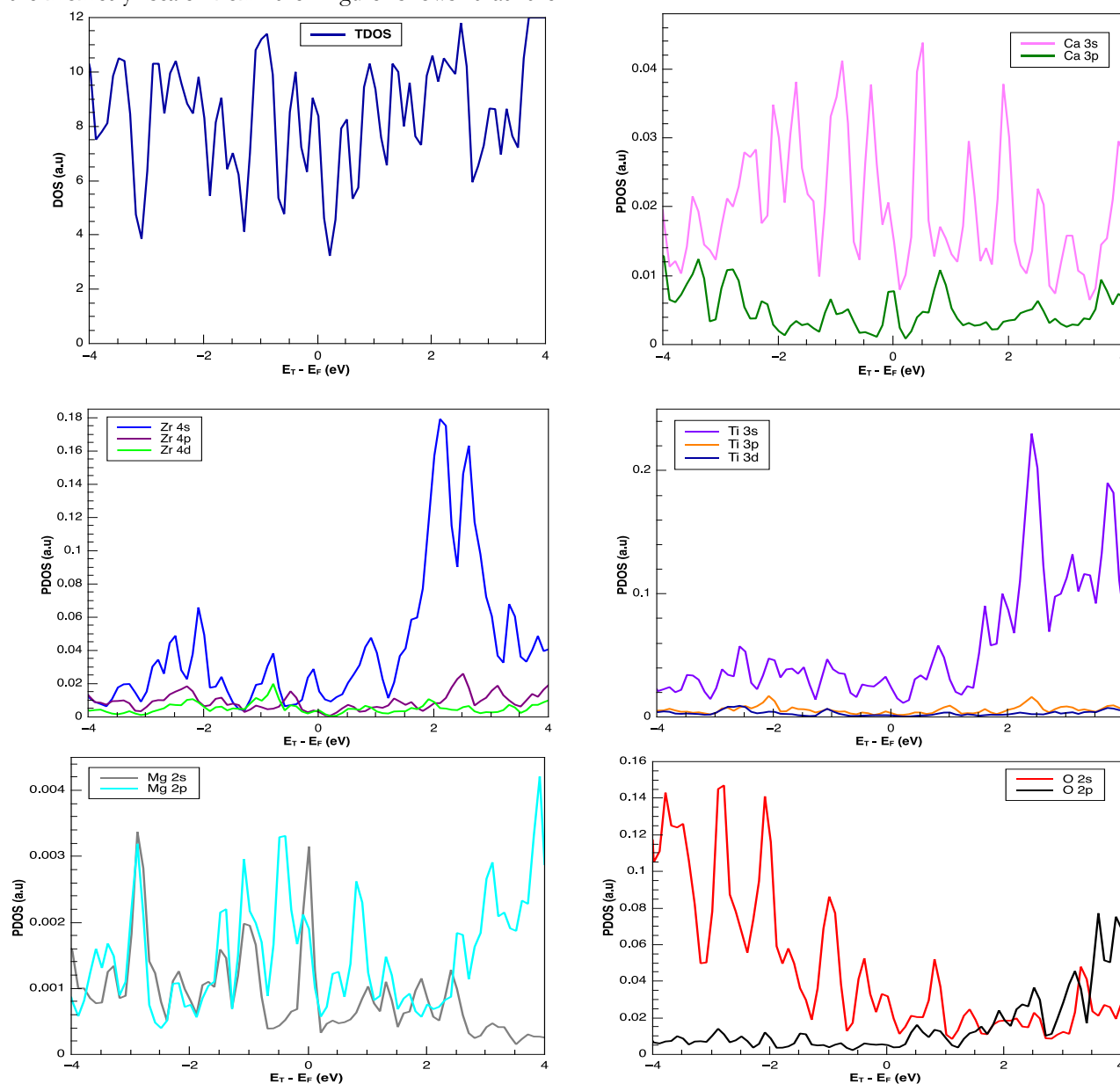
greater contribution was observed from  $Zr-4d$  and  $Ti-3d$  orbitals near the Fermi level. Therefore, these materials might have been responsible for the change in the material's properties.

**Table 3. The calculated energy gap of  $CaZrTi_2O_7$  and  $Mg$ -doped  $CaZrTi_2O_7$  with previous first principle calculations and experimental data.**

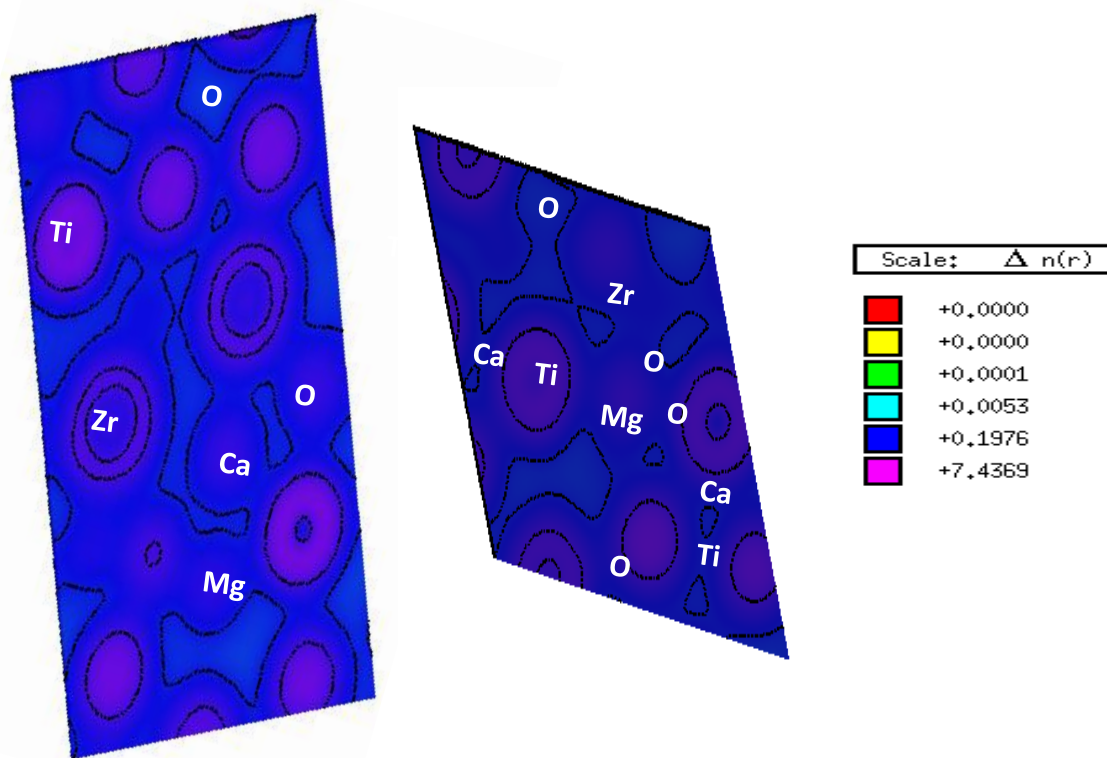
Material	Method	Bandgap E(eV)	Nature	Reference
Pure $CaZrTi_2O_7$	Experimental	3.60	Indirect	(Mulroue, 2013)
Pure $CaZrTi_2O_7$	Computational	2.90	Indirect	(Shuaibu <i>et al</i> , 2020)
$Mg$ -doped $CaZrTi_2O_7$	Computational	0.06	Indirect	This work

The charge density distribution has been plotted to understand the chemical bonding made by the atoms. The charge density distribution along the cations ( $Ca^{2+}$ ,  $Zr^{4+}$ ,  $Ti^{4+}$ , and  $Mg^{2+}$ ) are spherical, indicating charge transfer between the atoms, as shown in Figure 6. The plots indicate ionic bonding formed by the ions. The thermometry scale from the Figure shows that the

magenta color has the highest charge (+7.4369), which relates to the maximum charge accumulation of titanium atoms. However, the magnesium atom has a lower charge density (+0.1976). This indicates that titanium has the greatest charge density distribution in comparison to the remaining atoms.



**Figure 5. The total density of states and the partial density of states of  $Mg$  doped  $CaZrTi_2O_7$ .**



**Figure 6.** The charge density plot for the Magnesium (Mg) doped Zirconolite ( $\text{CaZrTi}_2\text{O}_7$ ) in different planes. The scale  $n(r)$  indicating ranges of isodensity values in atomic unit (a.u).

## CONCLUSION

The structural stability and electronic properties of Magnesium (Mg) doped Zirconolite ( $\text{CaZrTi}_2\text{O}_7$ ), which is the potential ceramic for Radioactive High-Level Waste immobilization, have been investigated using Quantum ESPRESSO Code within Density Functional Theory (DFT). A generalized gradient approximation (PBE-GGA) was used for total energy calculation. The Mg-doped  $\text{CaZrTi}_2\text{O}_7$  was confirmed based on an effective crystal plane model. A Mg atom substituted one of the Ti atoms on the surface of the zirconolite  $\text{CaZrTi}_2\text{O}_7$  crystal plane. The dopant substitution energy of Magnesium is computed to be  $1.424 \text{ eV}$ . The substitution energy acts as the degree of stability of the doped structure. The lower the substitution energy, the higher the stability of the structure. Based on the value obtained, Magnesium doped zirconolite  $\text{CaZrTi}_2\text{O}_7$  appears to be a stable structure. The electronic properties such as density of state (DOS), the partial density of state (PDOS), and band gap value of Mg-doped  $\text{CaZrTi}_2\text{O}_7$  were computed. The results reveal an indirect band gap energy of  $0.06 \text{ eV}$  which indicated its metallic behaviour. This band gap energy underestimation is due to the DFT approach limitation based on applied exchange-correlation functional. The findings indicate proper accommodation of Mg into Zirconolite which could enhanced an incorporation of

actinides/lanthanides into zirconolite structure. However, The Mg-doped Zirconolite could be investigated further for defect stability, vibrational stability and thermal properties.

## DECLARATION OF COMPETING INTEREST

The author declares no competing financial or personal interest to affect the work reported in this work.

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### APPENDIX A. SUPPLEMENTARY DATA

#### Convergence Test Results of Mg-doped Zirconolite

**Table A1: Convergence test of Mg-doped CaZrTi<sub>2</sub>O<sub>7</sub> based on total energy with respect to kinetic energy cut-off of the plane wave and total energy with respect to k-points grids.**

S/N	Convergence test	Kinetic energy cut-off (Ry)	Total energy (Ry)
1		20	-2456.36208243
2	Mg-doped CaZrTi <sub>2</sub> O <sub>7</sub> total energy	30	-2519.43384563
3	with respect to kinetic energy cut-off	40	-2524.98109508
4	of the plane wave.	50	-2525.27549136
5		60	-2525.32418651
6		70	-2525.35699485
		k-point mesh	Total energy (Ry)
1		2 × 2 × 2	-2525.27549136
2	Total energy with respect to the k-points	4 × 4 × 4	-2525.27791251
3	grids of Mg-doped CaZrTi <sub>2</sub> O <sub>7</sub> .	6 × 6 × 6	-2525.27914843
4		8 × 8 × 8	-2525.27905949
5		10 × 10 × 10	-2525.27913615
6		12 × 12 × 12	-2525.27910915